

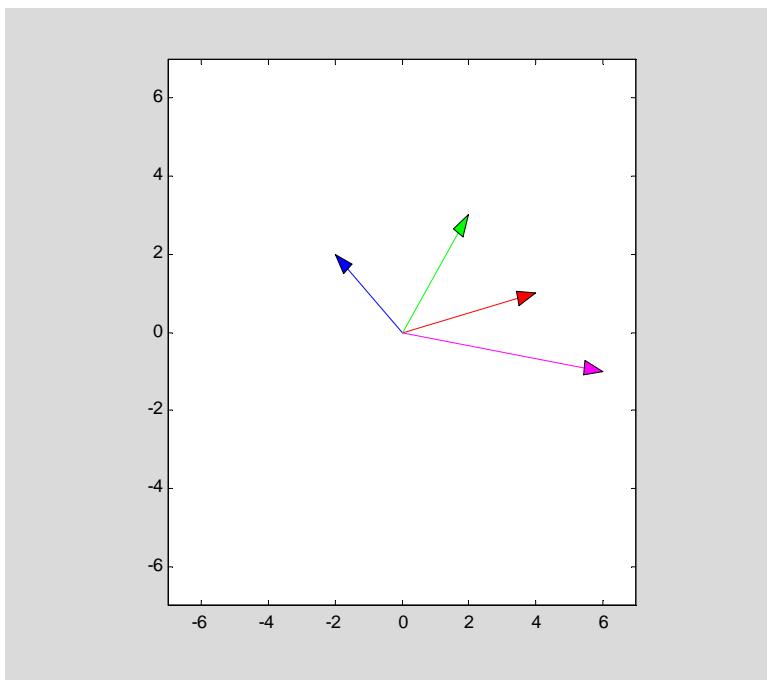
Key Homework 1

Strang Page 6 no: 1

```
v=[4; 1], w=[-2; 2]

v =
    4
    1
w =
   -2
    2

drawvec(v, 'red', 7); hold on, drawvec(w, 'blue', 7); hold on,
drawvec(v+w, 'green', 7); hold on, drawvec(v-w, 'magenta', 7);
```



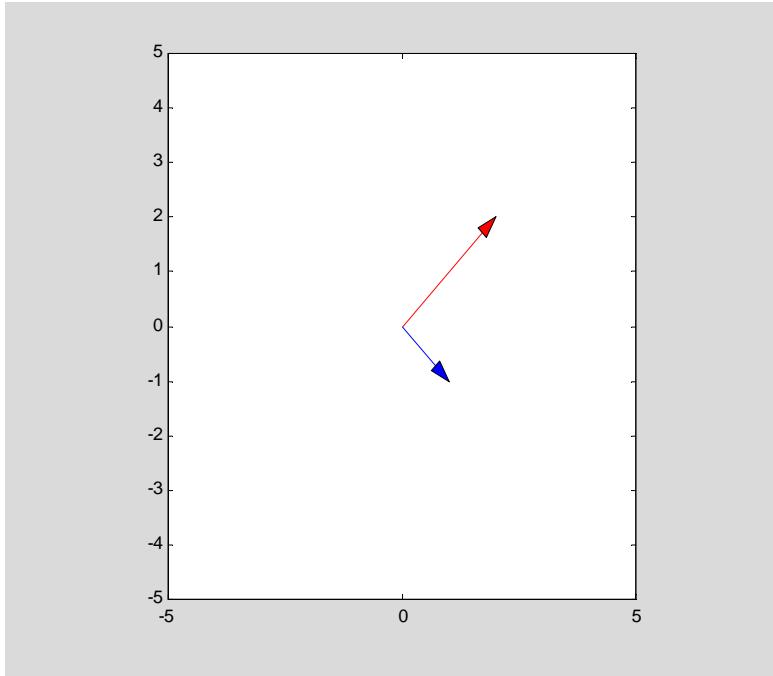
Strang Page 6 no: 2

a)
vPw=[3; 1], vMw=[1;3], v=(vPw+vMw)/2, w=(vPw-vMw)/2, drawvec(v, 'red');
hold on, drawvec(w, 'blue');

```

vPw =
  3
  1
vMw =
  1
  3
v =
  2
  2
w =
  1
 -1

```



Strang Page 6 no: 4

a)

```

u=[1; 2; 3], v=[-3; 1; -2], w=[2; -3; -1], ans1=u+v, ans2=u+v+w,
ans3=2*u+2*v+w

```

```

u =
  1
  2
  3
v =
 -3
  1
 -2
w =
  2
 -3
 -1
ans1 =
 -2
  3
  1

```

```

ans2 =
  0
  0
  0
ans3 =
 -2
  3
  1

```

Strang Page 6 no: 7

- a) First backward on w and then forward on v .
- b) The plane through u and v .

Strang Page 6 no: 11

a)

```

v=[4; 2], w=[-1; 2], left_side=norm(v, 2)^2+norm(w, 2)^2,
right_side=norm(v+w, 2)^2

```

```

v =
  4
  2
w =
 -1
  2
left_side =
 25.0000
right_side =
 25

```

- b) The formula fails if u and v are not perpendicular, for instance:

```

v=[5; 2], w=[-1; 2], left_side=norm(v, 2)^2+norm(w, 2)^2,
right_side=norm(v+w, 2)^2

```

```

v =
  5
  2
w =
 -1
  2
left_side =
 34
right_side =
 32.0000

```

Strang Page 6 no: 17

- a) This sum equals the vector $(0, 0)$.
- b) This sum equals negative the 4:00 vector.
- c) This sum equals negative one half of the 1:00 vector.

Strang Page 6 no: 29

$$c + 3d = 14$$

$$2c + d = 8$$

Strang Page 17 no: 2

```
u=[-0.6; 0.8], v=[3; 4], w=[4; 3]
```

```
u =
  -0.6000
  0.8000
v =
  3
  4
w =
  4
  3
```

Compute the lengths of the vectors.

```
Nu=norm(u, 2), Nv=norm(v, 2), Nw=norm(w, 2)
```

```
Nu =
  1
Nv =
  5
Nw =
  5
```

Check the Cauchy Schwarz inequalities $|u \bullet v| - \|u\| \|v\| \leq 0$ and $|v \bullet w| - \|v\| \|w\| \leq 0$.

```
check1=abs(u'*v)-Nu*Nv, check2=abs(v'*w)-Nv*Nw

check1 =
 -3.6000
check2 =
 -1
```

Strang Page 17 no: 7

- If $w = (w_1, w_2)$ is to be perpendicular to $v = (2, -1)$, then the dot product of the two vectors needs to equal zero. $\Rightarrow 2w_1 - w_2 = 0 \Rightarrow w_2 = 2w_1$. So we can write all vectors perpendicular to v as $w = \alpha(1, 2)$.
- All vectors perpendicular to $V = (1, 1, 1)$, constitute a plane through the origin and perpendicular to the vector V .

Strang Page 17 no: 13

For instance the $v = (1, 0, -1)$, and $w = (1, -2, 1)$.

Strang Page 17 no: 19

$$\begin{aligned}\|v + w\|^2 &= (v + w) \bullet (v + w) = \|v\|^2 + 2(v \bullet w) + \|w\|^2 \\ &\leq \|v\|^2 + 2|v \bullet w| + \|w\|^2 \leq \|v\|^2 + 2\|v\|\|w\| + \|w\|^2 = (\|v\| + \|w\|)^2.\end{aligned}$$

Taking the square root of both sides yields the triangle inequality $\|v + w\| \leq \|v\| + \|w\|$